

X8

HW: Quadratic Formula**Date: Dec. 18****Directions: Glue at the top of page 72**

- Solve each equation using the quadratic formula, write out the formula for each problem.
- Be sure to show all steps and substitution. Use pages 73 – 75.

1.) $4x^2 + 11x - 20 = 0$

$$\begin{aligned} a &= \underline{4} \\ b &= \underline{11} \\ c &= \underline{-20} \end{aligned}$$

Substitute in the values of a, b, and c into the quadratic formula.

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

$$x = \frac{-(\underline{11}) \pm \sqrt{(\underline{11})^2 - 4(4)(-20)}}{2(4)}$$

$$x = \frac{-11 \pm \sqrt{441}}{8} \rightarrow \frac{-11+21}{8} = \frac{5}{4}$$

$$\frac{-11-21}{8} = -4$$

The roots are: $\frac{5}{4}, -4$

3.) $x^2 = 3x + 3$

4.) $x^2 + 5 = -5x$

7.) The product of two consecutive odd integers is 99. Find the integers.

2.) $x^2 - 5x - 24 = 0$

$$\begin{aligned} a &= \underline{1} \\ b &= \underline{-5} \\ c &= \underline{-24} \end{aligned}$$

Substitute in the values of a, b, and c into the quadratic formula.

$$x = \frac{-(-5) \pm \sqrt{(-5)^2 - 4(1)(-24)}}{2(1)}$$

$$x = \frac{5 \pm \sqrt{121}}{2} \rightarrow \frac{5+11}{2} = 8$$

$$x = \frac{5 \pm 11}{2} = \frac{5-11}{2} = -3$$

The roots are: $8, -3$

5.) $4x^2 + 7x - 15 = 0$

6.) $x^2 = 10 - 3x$

8.) Find two consecutive positive integers such that the square of the first is decreased by 17 equals 4 times the second.

3.) $x^2 - 3x - 3 = 0$ $a = 1, b = \underline{-3}, c = \underline{-3}$

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

$$x = \frac{-(-3) \pm \sqrt{(-3)^2 - 4(1)(-3)}}{2(1)}$$

$$x = \frac{3 \pm \sqrt{21}}{2} = \frac{3 + \sqrt{21}}{2} \approx 3.79128\dots$$

$$\frac{3 - \sqrt{21}}{2} \approx -0.79128\dots$$

4.) $x^2 + 5x + 5 = 0$

$a = 1$

$b = 5$

$c = 5$

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

roots/zeros

$$x = \frac{-5 \pm \sqrt{5}}{2}$$

$$x = \frac{-5 \pm \sqrt{(5)^2 - 4(1)(5)}}{2(1)}$$

$$\begin{aligned} \frac{-5 + \sqrt{5}}{2} &\approx 1.3819\dots \\ \frac{-5 - \sqrt{5}}{2} &\approx -3.6180\dots \end{aligned}$$

5.) $4x^2 + 7x - 15 = 0$

$a = 4$

$b = 7$

$c = -15$

$$x = \frac{-7 \pm \sqrt{7^2 - 4(4)(-15)}}{2(4)}$$

$$x = \frac{-7 \pm \sqrt{289}}{8} = \begin{cases} \frac{-7 + 17}{8} = \frac{10}{8} = \frac{5}{4} \\ \frac{-7 - 17}{8} = \frac{-24}{8} = -3 \end{cases}$$

$$x = \left\{ -3, \frac{5}{4} \right\}$$

roots/zeros

6.) $x^2 = 10 - 3x$

$-10 + 3x$

$a = 1$

$x^2 + 3x - 10 = 0$

$b = 3$

$c = -10$

$$x = \frac{-3 \pm \sqrt{3^2 - 4(1)(-10)}}{2(1)}$$

$$x = \frac{-3 \pm \sqrt{49}}{2} = \begin{cases} \frac{-3 + 7}{2} = 2 \\ \frac{-3 - 7}{2} = -5 \end{cases}$$

$$x = \left\{ 2, -5 \right\}$$

roots/zeros

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7.) Let 1st COI = x
 2nd COI = $x + 2$

$$x(x+2) = 99$$

$$\begin{array}{r} x^2 + 2x = 99 \\ -99 \quad -99 \\ \hline x^2 + 2x - 99 = 0 \end{array}$$

$$a = 1, b = 2, c = -99$$

$$x = \frac{-2 \pm \sqrt{(2)^2 - 4(1)(-99)}}{2(1)}$$

$$x = \frac{-2 \pm \sqrt{400}}{2} = \frac{-2 \pm 20}{2}$$

$$\begin{matrix} -2+20 \\ 2 \\ -9 \end{matrix} \quad \left\{ \quad \begin{matrix} -2-20 \\ 2 \\ -11 \end{matrix} \right.$$

answer:

$$\text{1st } \# = 9 \\ \text{2nd } \# = 11$$

$$\text{or} \\ \text{1st } \# = -11 \\ \text{2nd } \# = -9$$

8.) Let 1st CPI = x
 2nd CPI = $x + 1$

$$x^2 - 17 = 4(x+1)$$

$$a=1$$

$$x^2 - 17 = 4x + 4$$

$$b=-4$$

$$-4x - 4 - 4x - 4$$

$$c=-21$$

$$x^2 - 4x - 21 = 0$$

$$x = \frac{-(-4) \pm \sqrt{(-4)^2 - 4(1)(-21)}}{2(1)}$$

$$x = \frac{4 \pm \sqrt{100}}{2} = \frac{4 \pm 10}{2}$$

$$\frac{-4+10}{2} \quad \left\{ \quad \frac{-4-10}{2}$$

$$3$$

\cancel{x} reject
 b/c it wants
 a positive
 integer

ANSWER:

$$1st \# = 3$$

$$2nd \# = 4$$