

Definitions:

1.) **Consecutive Integers (CI):** are integers that follow one another in order. They have a difference of 1 between every two numbers.

Ex: 1, 2, 3, 4, 5, 6, . . . **algebra:** $n, n + 1, n + 2, \dots$

2) **Consecutive Even Integers (CEI):** are integers that follow one another in order. They have a difference of 2 between every two numbers.

Ex: 2, 4, 6, 8, 10, . . . **algebra:** $n, n + 2, n + 4, \dots$

3.) **Consecutive Odd Integers (COI):** are integers that follow one another in order. They have a difference of 2 between every two numbers.

Ex: 1, 3, 5, 7, 9, . . . **algebra:** $n, n + 2, n + 4, \dots$

Example

1.) Find two consecutive integers whose sum is 95.

Let 1st CI = $x = 47$
2nd CI = $x + 1 = 47 + 1 = 48$

$(1^{st} CI) + (2^{nd} CI) = 95$

Equation: $x + x + 1 = 95$

$$\begin{array}{r} x + x + 1 = 95 \\ 2x + 1 = 95 \\ \underline{-1 \quad -1} \\ 2x = 94 \\ \underline{ } \\ x = 47 \end{array}$$

Example

2.) Find three consecutive positive even integers such that 4 times the first decreased by the second is 12 more than twice the third.

Let 1st CEI = $x = 22$
2nd CEI = $x + 2 = 22 + 2 = 24$
3rd CEI = $x + 4 = 22 + 4 = 26$

$4(1^{st} CEI) - (2^{nd} CEI) = 2(3^{rd} CEI) + 12$

Equation: $4x - (x + 2) = 2(x + 4) + 12$

$$\begin{array}{r} 4x - (x + 2) = 2(x + 4) + 12 \\ 4x - x - 2 = 2x + 8 + 12 \\ 3x - 2 = 2x + 20 \\ \underline{-2x \quad -2x} \\ x - 2 = 20 \\ \underline{+2 \quad +2} \\ x = 22 \end{array}$$

Example

3.) Find three consecutive odd integers such that the largest decreased by 3 times the second is 47 less than the smallest.

Let 1st COI = $x = 15$
2nd COI = $x + 2 = 15 + 2 = 17$
3rd COI = $x + 4 = 15 + 4 = 19$
 $3^{rd} - 3(2^{nd}) = 1^{st} - 47$

Equation: $x + 4 - 3(x + 2) = x - 47$

$$\begin{array}{r} x + 4 - 3(x + 2) = x - 47 \\ x + 4 - 3x - 6 = x - 47 \\ -2x - 2 = x - 47 \\ \underline{+2x \quad +2x} \\ -2 = 3x - 47 \\ \underline{+47 \quad +47} \\ 45 = 3x \\ \underline{ } \\ x = 15 \end{array}$$